

# Teoria e fenomenologia dei modelli di Higgs composto

---

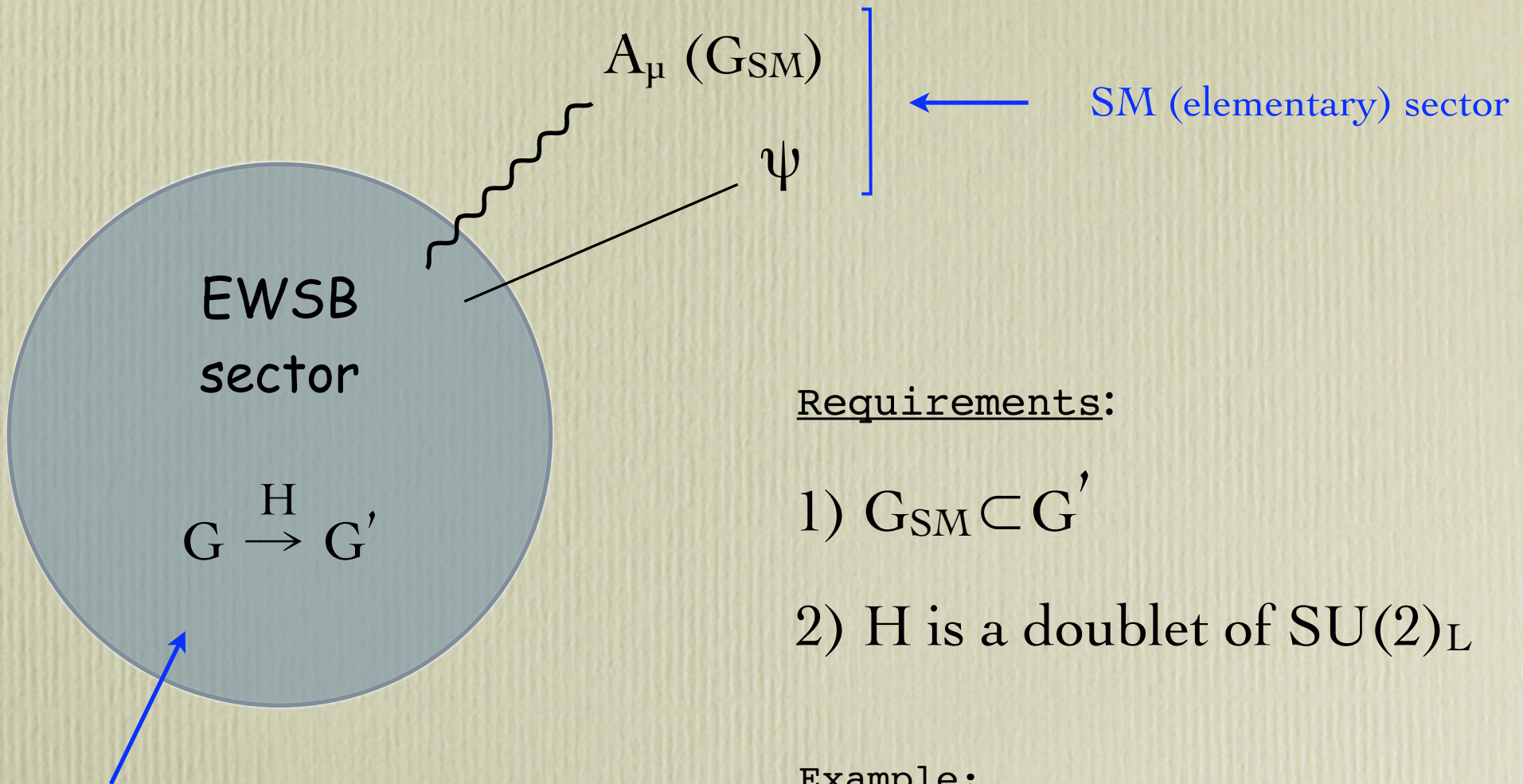
Roberto Contino - CERN

# **PART I:**

Quick review of the Composite Higgs

# Composite Higgs models

[Georgi & Kaplan, '80s]



EWSB sector characterized by:

$$m_\rho \quad g_{SM} \lesssim g_\rho \lesssim 4\pi$$

(derived scale:  $f = m_\rho/g_\rho$ )

Requirements:

- 1)  $G_{SM} \subset G'$
- 2)  $H$  is a doublet of  $SU(2)_L$

Example:

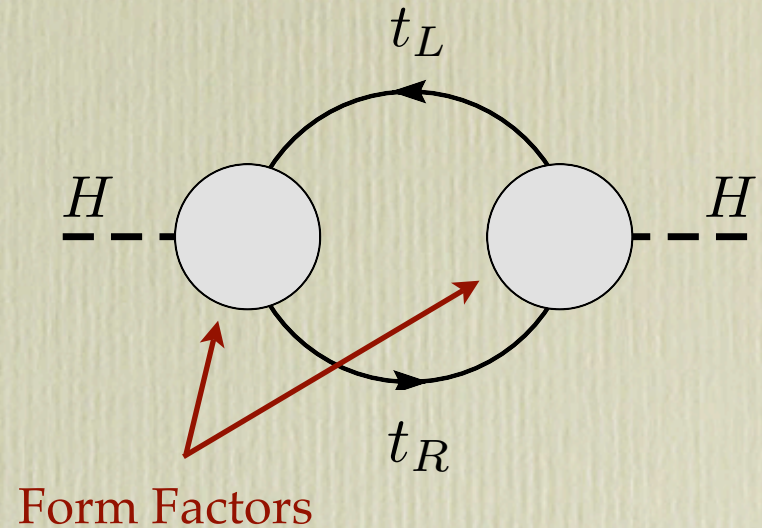
$$SO(5) \rightarrow SO(4) \sim SU(2)_L \times SU(2)_R$$

gives 4 real Goldstones: one  $SU(2)_L$  doublet  $H$

# 1-loop potential for the pseudo-Goldstone Higgs

only loops with virtual elementary fields generate a potential

Higgs couplings switch off at large momenta  $\rightarrow$  finiteness

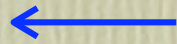


periodic function ( $H \in G/G'$ )

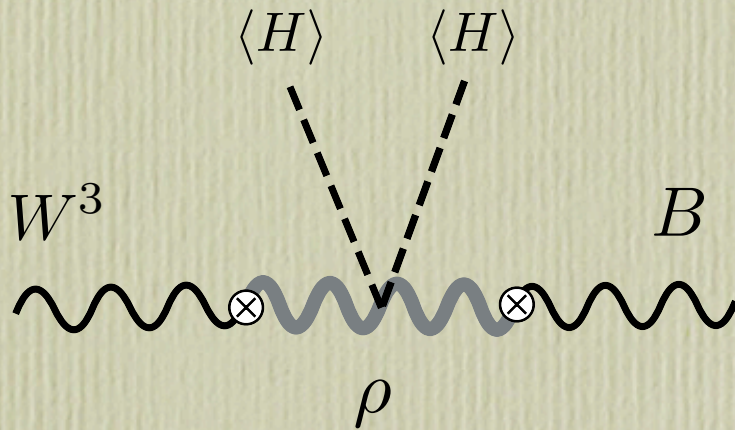
$$V(h) \approx \frac{3 y_t^2}{16\pi^2} m_\rho^2 f^2 \zeta(h/f)$$

$$\lambda_4 \sim \frac{3}{16\pi^2} y_t^2 g_\rho^2$$

$$\xi = \left( \frac{v}{f} \right)^2$$



new parameter compared to TC  
(fixed by the dynamics)



$$S \sim 16\pi \left( \frac{v}{m_\rho} \right)^2 \sim \xi \frac{N}{\pi}$$

$m_\rho \sim \frac{4\pi f}{\sqrt{N}}$

$$\xi \rightarrow 0$$

$$[f \rightarrow \infty]$$

decoupling limit:

All  $\rho$ 's become heavy and  
one re-obtains the SM

# Constraint on the strong sector from the LEP precision tests :

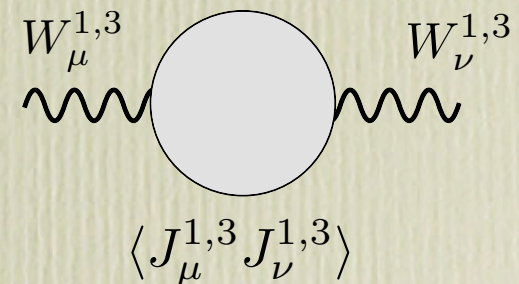
## Custodial Symmetry

$$\rho = \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} \quad \Delta\rho \equiv (\rho - 1) = \frac{4}{v^2} [\Pi_{11}(0) - \Pi_{33}(0)]$$

- The bound from LEP  $\Delta\rho \lesssim 2 \times 10^{-3}$  strongly constrains tree-level corrections

- If the residual symmetry after EWSB is just  $U(1)_Q$  there will be tree-level corrections from the strong sector to  $\Delta\rho$

$$\langle J_\mu^1 J_\nu^1 \rangle \neq \langle J_\mu^3 J_\nu^3 \rangle$$



- A larger preserved “custodial” symmetry  $SU(2)_C$  under which  $J_\mu^i$  transforms like a triplet can protect  $\Delta\rho$

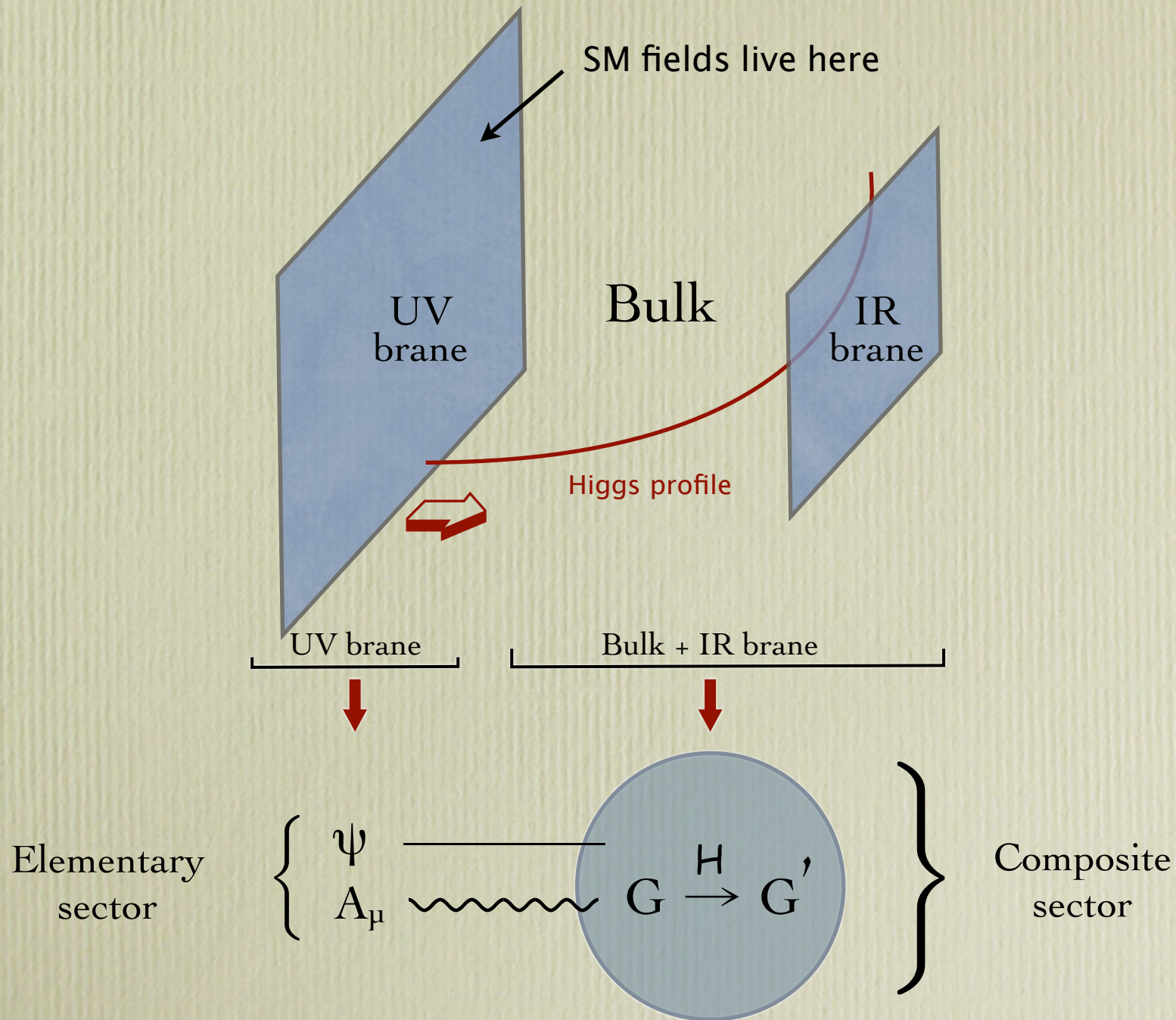
[Sikivie et al. NPB 173 (1980) 189]

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_C$$



$$\langle J_\mu^1 J_\nu^1 \rangle = \langle J_\mu^3 J_\nu^3 \rangle$$

# Equivalence with 5D warped field theories:



# PART II:

## Implications for the LHC

1. How to tell whether the Higgs is composite
2. Direct production of new states



# An effective Lagrangian for the Strongly Interacting Light Higgs

built along the rules of the chiral expansion:

Giudice, Grojean, Pomarol, Rattazzi  
JHEP 0706:045 (2007)

1. each extra Goldstone leg is weighted by a factor  $1/f$
2. each derivative is weighted by a factor  $1/m_\rho$
3. higher dimensional operators that violate the symmetry of the  $\sigma$ -model must be suppressed by  $g_{SM}$

at the level of dimension-6 operators:

strong constraint from LEP

$$\Delta\rho = c_T \xi$$

$$\mathcal{L}_{\text{SILH}} = \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{c_T}{2f^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) \left( H^\dagger \overleftrightarrow{D}_\mu H \right) - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3 + \left( \frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.} \right)$$

probe  
strong  
coupling

$$+ \frac{ic_W g}{2m_\rho^2} \left( H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i + \frac{ic_B g'}{2m_\rho^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu})$$

1-loop  
suppressed

$$+ \frac{ic_{HW} g}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{ic_{HB} g'}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

more than  
1-loop  
suppressed

$$+ \frac{c_\gamma g'^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$$

form  
factors

dominant effect:

shift in the Higgs couplings

subdominant role in scattering amplitudes

one combination

constrained by LEP:

$$\hat{S} = (c_W + c_B) \frac{m_W^2}{m_\rho^2}$$

$$\begin{aligned} \mathcal{L}_{\text{SILH}} = & \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{c_T}{2f^2} \left( H^\dagger \overleftarrow{D}^\mu H \right) \left( H^\dagger \overrightarrow{D}_\mu H \right) \\ & - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3 + \left( \frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.} \right) \\ & + \frac{ic_W g}{2m_\rho^2} \left( H^\dagger \sigma^i \overleftarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i + \frac{ic_B g'}{2m_\rho^2} \left( H^\dagger \overleftarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu}) \\ & + \frac{ic_{HW} g}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{ic_{HB} g'}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ & + \frac{c_\gamma g'^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu} \end{aligned}$$

directly affect Higgs gluon production  
and Higgs decay to photons

(subdominant compared to  $c_H$ )

# shifts in the Higgs couplings:

$$\Gamma(h \rightarrow f\bar{f})_{\text{SILH}} = \Gamma(h \rightarrow f\bar{f})_{\text{SM}} [1 - \xi(2c_y + c_H)]$$

$$\Gamma(h \rightarrow W^+W^-)_{\text{SILH}} = \Gamma(h \rightarrow W^+W^{(*)-})_{\text{SM}} \left[ 1 - \xi \left( c_H - \frac{g^2}{g_\rho^2} \hat{c}_W \right) \right]$$

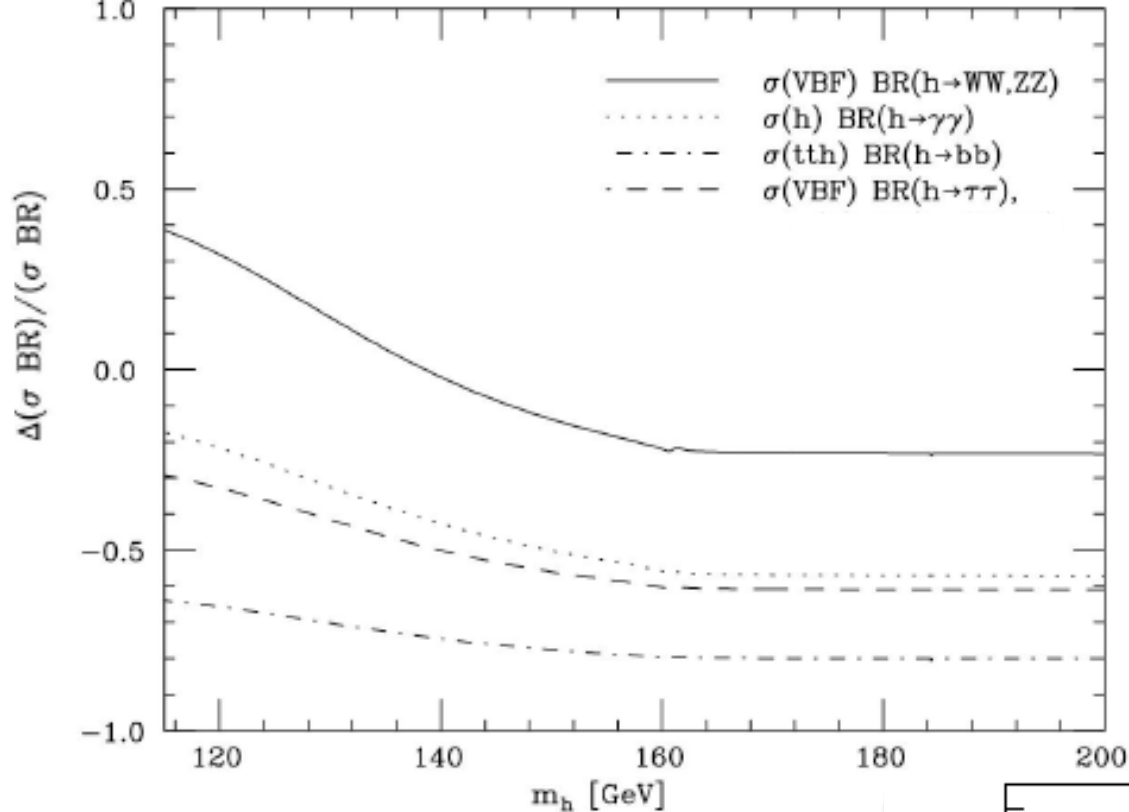
$$\Gamma(h \rightarrow ZZ)_{\text{SILH}} = \Gamma(h \rightarrow ZZ^{(*)})_{\text{SM}} \left[ 1 - \xi \left( c_H - \frac{g^2}{g_\rho^2} \hat{c}_Z \right) \right]$$

$$\Gamma(h \rightarrow gg)_{\text{SILH}} = \Gamma(h \rightarrow gg)_{\text{SM}} \left[ 1 - \xi \operatorname{Re} \left( 2c_y + c_H + \frac{4y_t^2 c_g}{g_\rho^2 I_g} \right) \right]$$

$$\Gamma(h \rightarrow \gamma\gamma)_{\text{SILH}} = \Gamma(h \rightarrow \gamma\gamma)_{\text{SM}} \left[ 1 - \xi \operatorname{Re} \left( \frac{2c_y + c_H}{1 + J_\gamma/I_\gamma} + \frac{c_H - \frac{g^2}{g_\rho^2} \hat{c}_W}{1 + I_\gamma/J_\gamma} + \frac{\frac{4g^2}{g_\rho^2} c_\gamma}{I_\gamma + J_\gamma} \right) \right]$$

$$\Gamma(h \rightarrow \gamma Z)_{\text{SILH}} = \Gamma(h \rightarrow \gamma Z)_{\text{SM}} \left[ 1 - \xi \operatorname{Re} \left( \frac{2c_y + c_H}{1 + J_Z/I_Z} + \frac{c_H - \frac{g^2}{g_\rho^2} \hat{c}_W}{1 + I_Z/J_Z} + \frac{4c_{\gamma Z}}{I_Z + J_Z} \right) \right]$$

$$\left[ \hat{c}_W = c_W + \left( \frac{g_\rho}{4\pi} \right)^2 c_{HW}, \quad \hat{c}_Z = \hat{c}_W + \tan^2 \theta_W \left[ c_B + \left( \frac{g_\rho}{4\pi} \right)^2 c_{HB} \right], \quad c_{\gamma Z} = \frac{c_{HB} - c_{HW}}{4 \sin 2\theta_W} \right]$$



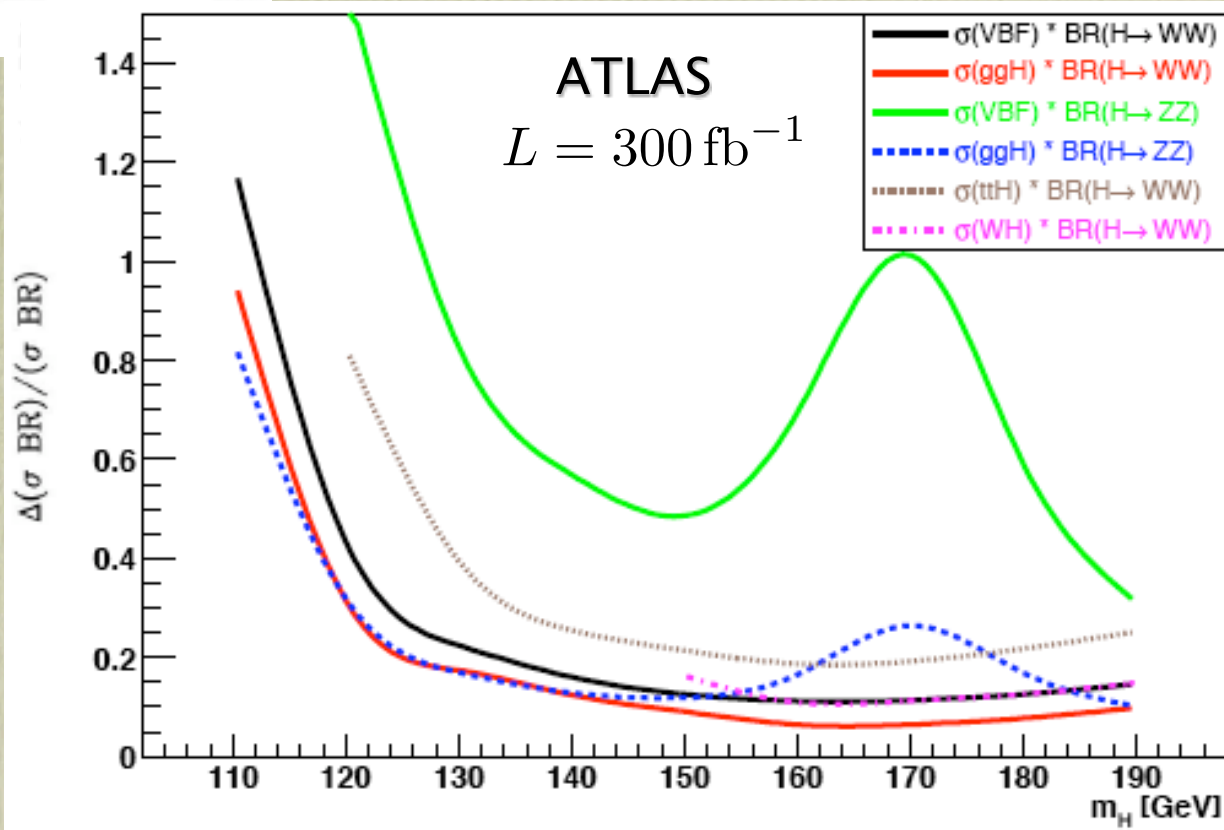
prediction of the  $\text{SO}(5)/\text{SO}(4)$  model [ $c_y/c_H = 1$ ] for  $c_H \xi = 0.25$

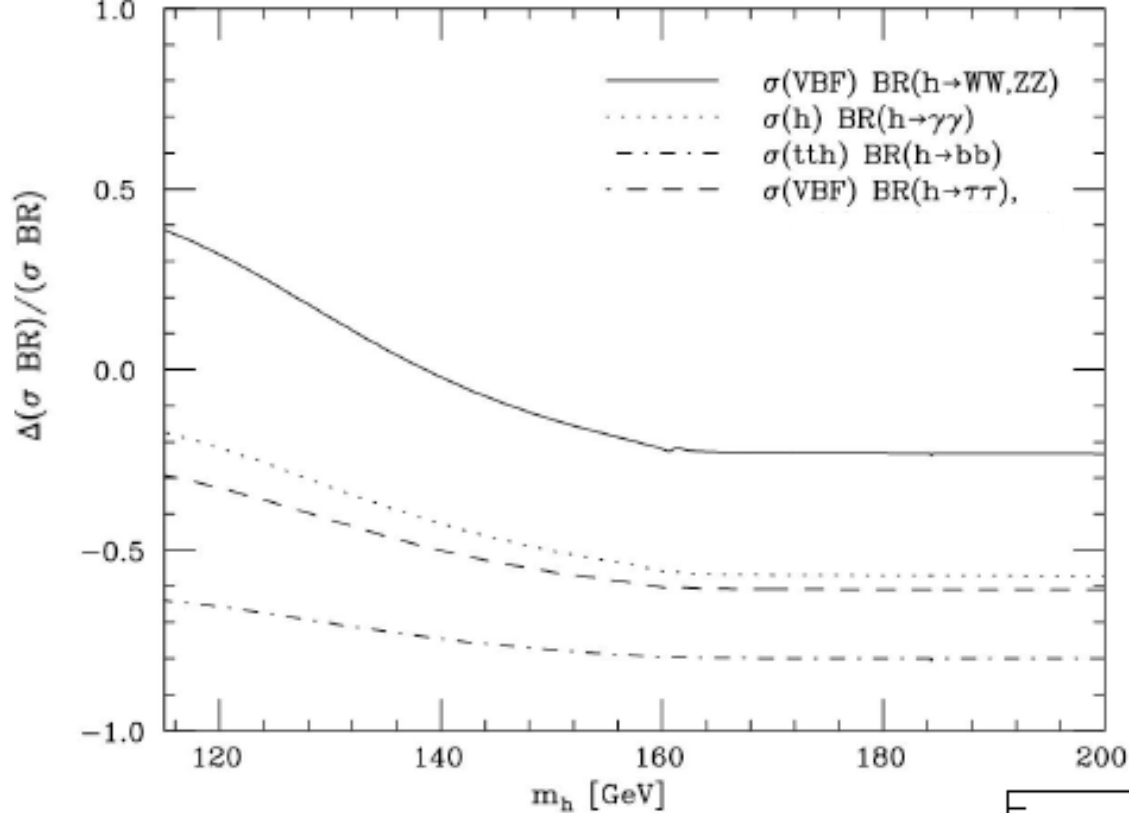
[ Giudice et al. JHEP 0706:045, 2007 ]

LHC sensitive up to

$c_H \xi = 0.2 - 0.4$

[ Duhrssen ATL-PHYS-2003-030 ]





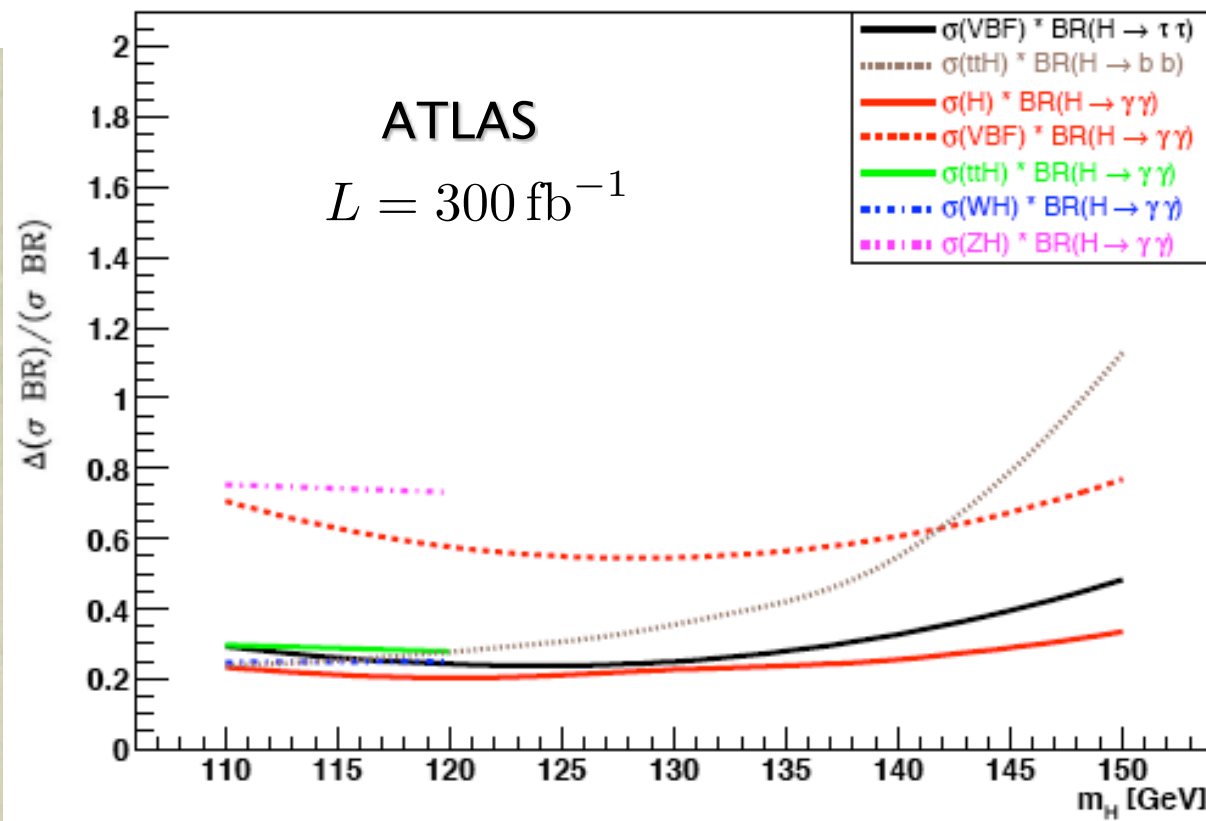
prediction of the SO(5)/SO(4) model [ $c_y/c_H = 1$ ] for  $c_H \xi = 0.25$

[ Giudice et al. JHEP 0706:045, 2007 ]

LHC sensitive up to

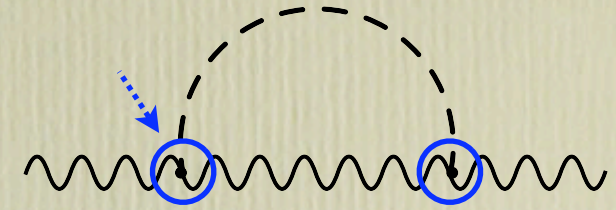
$c_H \xi = 0.2 - 0.4$

[ Duhrssen ATL-PHYS-2003-030 ]



☞ as stressed in: Barbieri et al. PRD 76 (2007) 115008

the shifts in the Higgs couplings induce an IR correction to the precision parameters  $\epsilon_{1,3}$



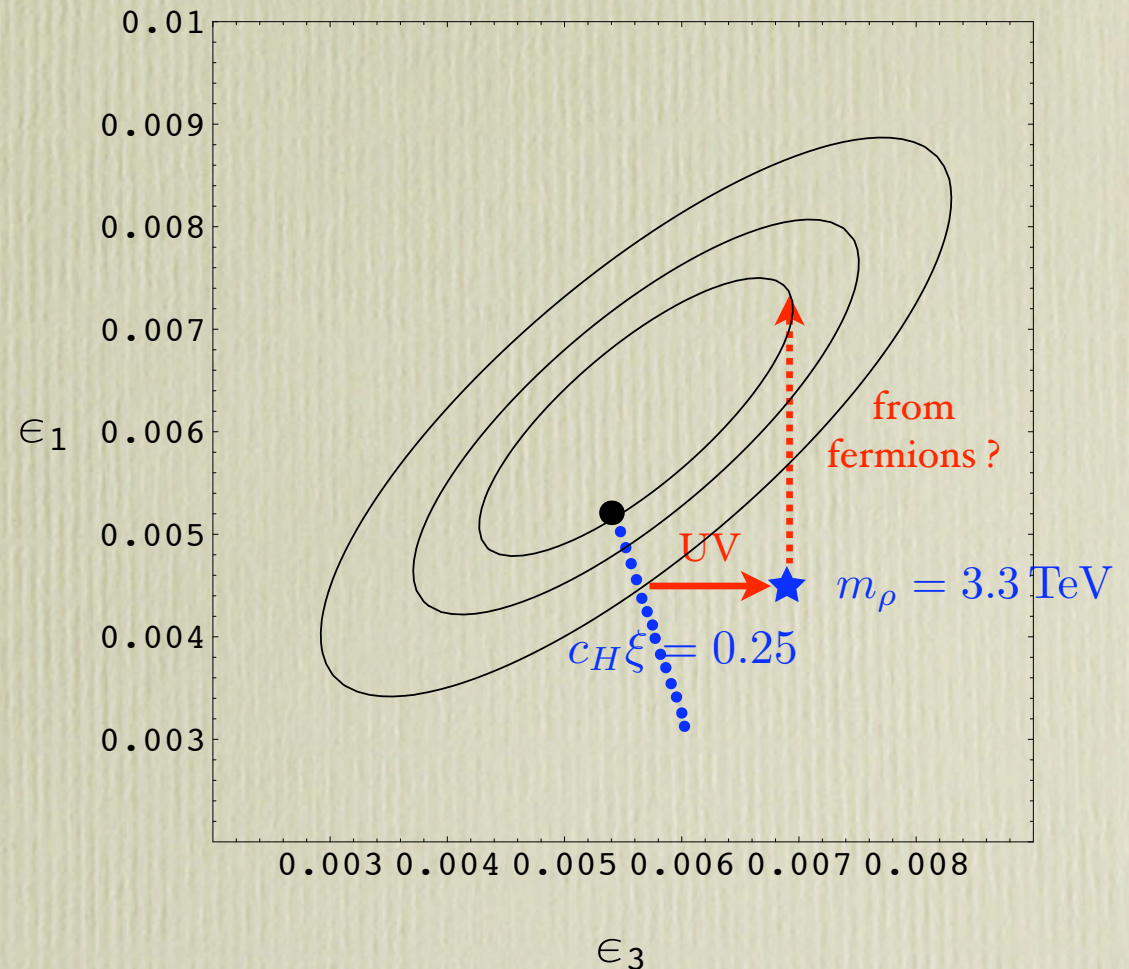
$$\epsilon_{1,3} = a_{1,3} \log \left( \frac{M_Z^2}{\mu^2} \right) - a_{1,3} (1 - c_H \xi) \log \left( \frac{m_h^2}{\mu^2} \right) - a_{1,3} (c_H \xi) \log \left( \frac{m_\rho^2}{\mu^2} \right) + \text{finite terms}$$

$$a_1 = + \frac{3}{16\pi} \frac{\alpha(M_Z)}{\cos^2 \theta_W}$$

$$a_3 = - \frac{1}{12\pi} \frac{\alpha(M_Z)}{4 \sin^2 \theta_W}$$

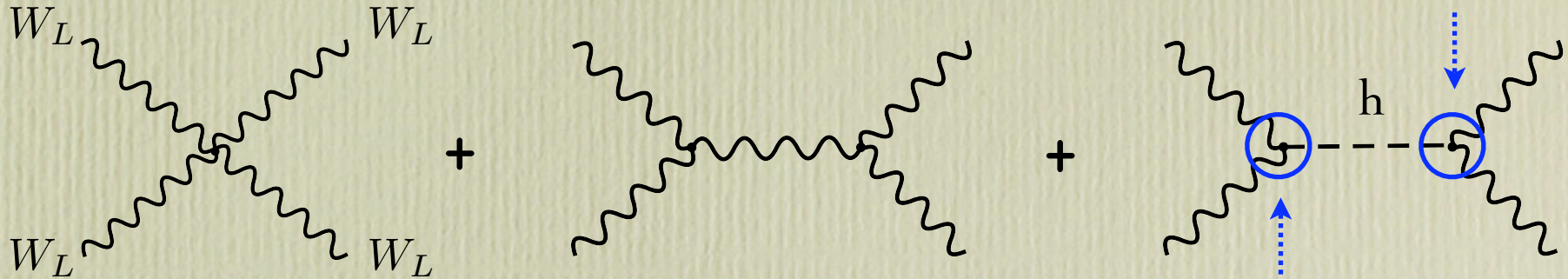
$$\Delta \epsilon_1 = a_1 (c_H \xi) \log \left( \frac{m_h^2}{m_\rho^2} \right)$$

$$\Delta \epsilon_3 = a_3 (c_H \xi) \log \left( \frac{m_h^2}{m_\rho^2} \right)$$



# WW scattering

- The Higgs compositeness implies a **partial unitarization** of the WW scattering:



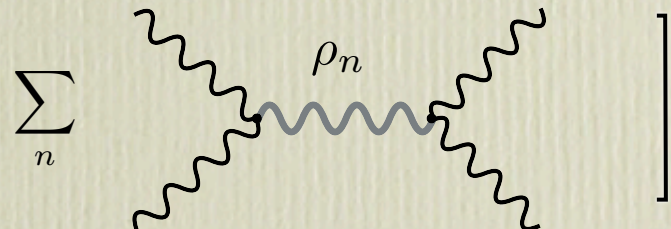
$$A(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = \frac{g_2^2}{4M_W^2} \left[ s - \frac{s^2 (1 - c_H \xi)}{s - m_h^2} + t - \frac{t^2 (1 - c_H \xi)}{t - m_h^2} \right]$$

Unitarity is lost at a scale:

$$\Lambda = \Lambda_0 / \sqrt{c_H \xi}$$

$\Lambda_0 = 1.2 \text{ TeV}$

Full unitarity is recovered thanks to the exchange of the heavy vectorial resonances





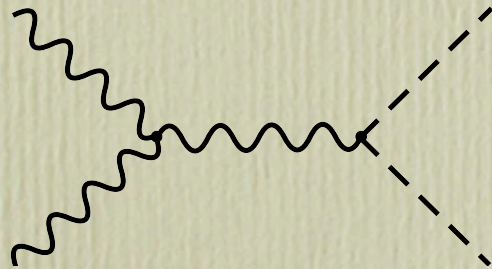
- At large invariant ( $WW$ ) masses one case thus rescale:

$$\sigma(pp \rightarrow V_L V'_L X)_{c_H \xi} \simeq (c_H \xi)^2 \sigma(pp \rightarrow V_L V'_L X)_{\text{no Higgs}}$$

with  $L = 200 \text{ fb}^{-1}$  the LHC should be sensitive up to  $c_H \xi = 0.5 - 0.7$

[ Giudice et al. JHEP 0706:045, 2007 ]

- Strong vector boson scattering is accompanied by **strong Higgs production**:



$$A(Z_L Z_L \rightarrow hh) = A(W_L^+ W_L^- \rightarrow hh) = \frac{s}{v^2} (c_H \xi)$$



**WORK IN  
PROGRESS**

with C. Grojean, M. Moretti, F. Piccinini, R. Rattazzi

# PART II:

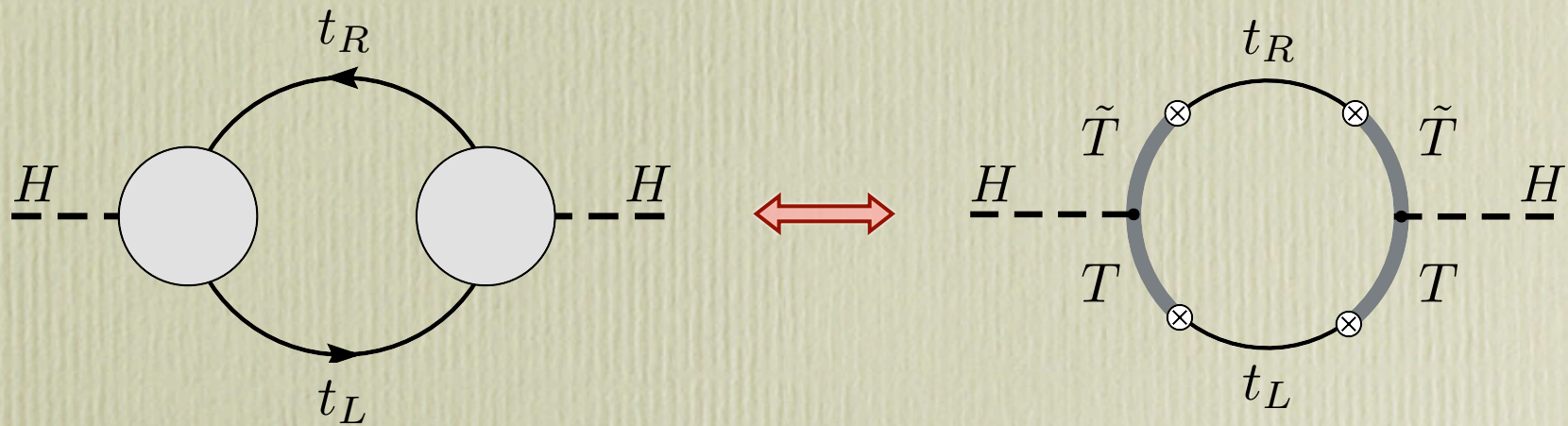
## Implications for the LHC

1. How to tell whether the Higgs is composite
2. Direct production of new states

# THE TOP PARTNERS

A light Higgs requires:

New vector-like quarks with  $M \sim 500$  GeV  
in multiplets of  $SU(2)_L \times SU(2)_R \times U(1)_X$



★ Two simple  $SU(2)_L \times SU(2)_R \times U(1)_X$  assignments:  $[ Y = T_{3_R} + X ]$

**Model A**

$$(\mathbf{2}, \mathbf{1})_{1/6} = \begin{pmatrix} T \\ B \end{pmatrix}$$

$$(\mathbf{1}, \mathbf{2})_{1/6} = \begin{pmatrix} \tilde{T} \\ \tilde{B} \end{pmatrix}$$

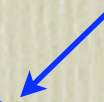
$$[ X = (B - L)/2 ]$$

**Model B**

$$(\mathbf{2}, \mathbf{2})_{2/3} = \begin{bmatrix} Q' = \begin{pmatrix} T_{5/3} \\ T_{2/3} \end{pmatrix} \\ Q = \begin{pmatrix} T \\ B \end{pmatrix} \end{bmatrix}$$

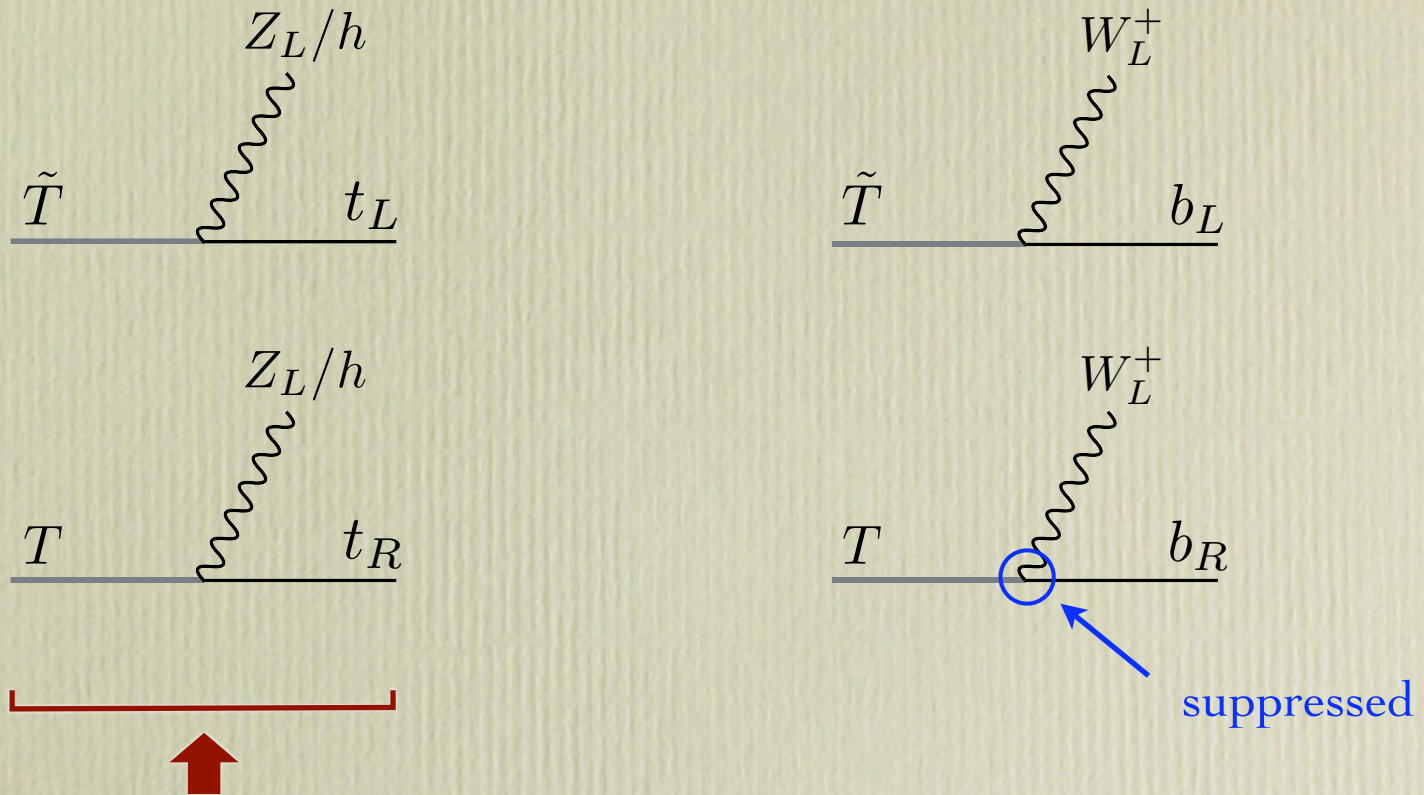
$$(\mathbf{1}, \mathbf{1})_{2/3} = \tilde{T}$$

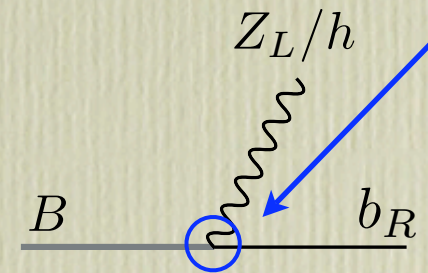
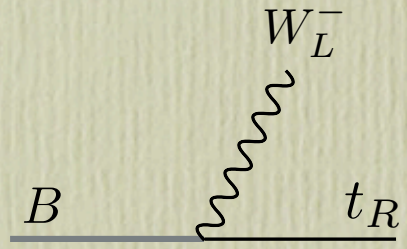
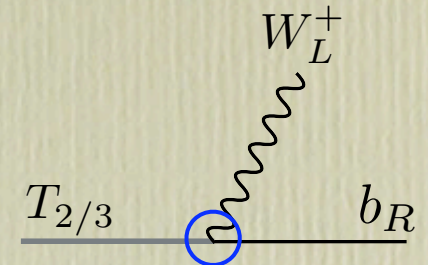
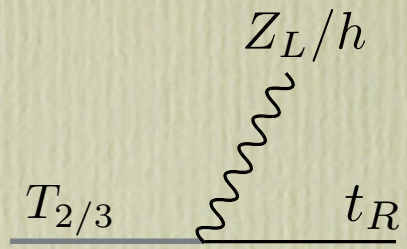
electric charge  $+5/3$



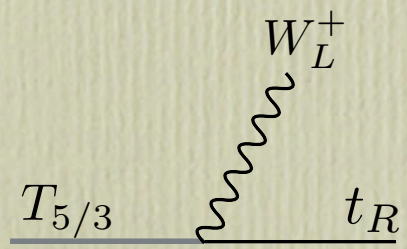
$$[ X = 2(B - L) ]$$

- ◆ largest coupling of the heavy fermions to the Higgs degrees of freedom ( $W_L, Z_L, h$ ) and to the SM third quark generation
- ◆ couplings to well defined SM quark chiralities [Yukawa couplings]





suppressed



Single production and decays proceed via these couplings

Pair production proceeds via the usual QCD coupling

✓ Production of the heavy tops ( $\tilde{T}, T, T_{2/3}$ ) has been studied in the literature:

◆ **Single production** via  $bW$  fusion  $\rightarrow$  best channel:  $\tilde{T} \rightarrow W^+ b \rightarrow l^+ \nu b$

LHC reach with  $L = 300 \text{ fb}^{-1}$ :  $M = 2 (2.5) \text{ TeV}$  for  $\lambda_T = 1 (2)$

see: Azuelos et al. Eur.Phys.J. C39S2 (2005) 13 [hep-ph/0402037]

◆ **Pair production**  $\rightarrow$  best channels:  $\tilde{T}\tilde{\bar{T}} \rightarrow \begin{cases} W^+ b W^- \bar{b} \\ W^+ b h \bar{t} \\ W^+ b Z \bar{t} \end{cases} \rightarrow$  final states with **1 charged lepton**

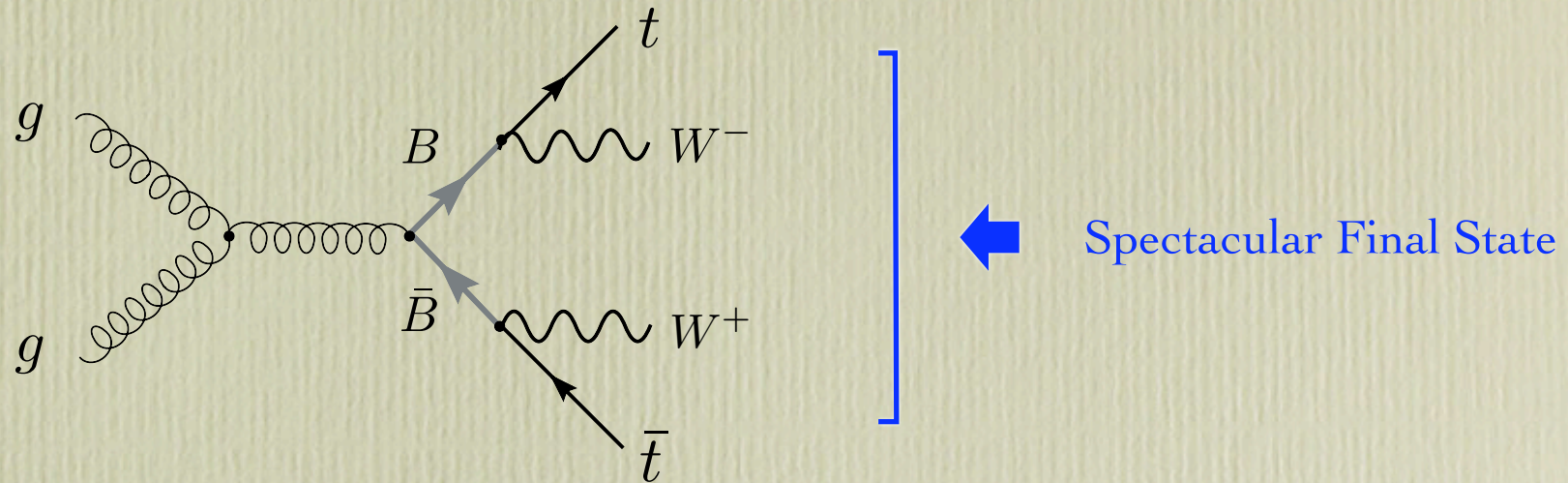
$L_{disc} = 2.1(90) \text{ fb}^{-1}$  for  $M_{\tilde{T}} = 0.5(1) \text{ TeV}$

see: J.A. Aguilar-Saavedra PoS TOP2006:003,2006 [hep-ph/0603199] and refs. therein

□ Pair production of the heavy bottom ( $B$ ) has also been investigated recently:

Skiba and Tucker-Smith PRD 75 (2007) 115010

C. Dennis et al. hep-ph/0701158



- channels investigated:  $l^\pm + jets + \cancel{E}_T$  and  $l^+l^- + jets + \cancel{E}_T$

➔ Challenge:  $t\bar{t} + jets$  huge background ➔ hard cuts on  $M_{\text{eff}}$  needed

- additional strategy proposed by Skiba and Tucker-Smith : look for highly boosted tops and Ws and cut on **single jet invariant mass**

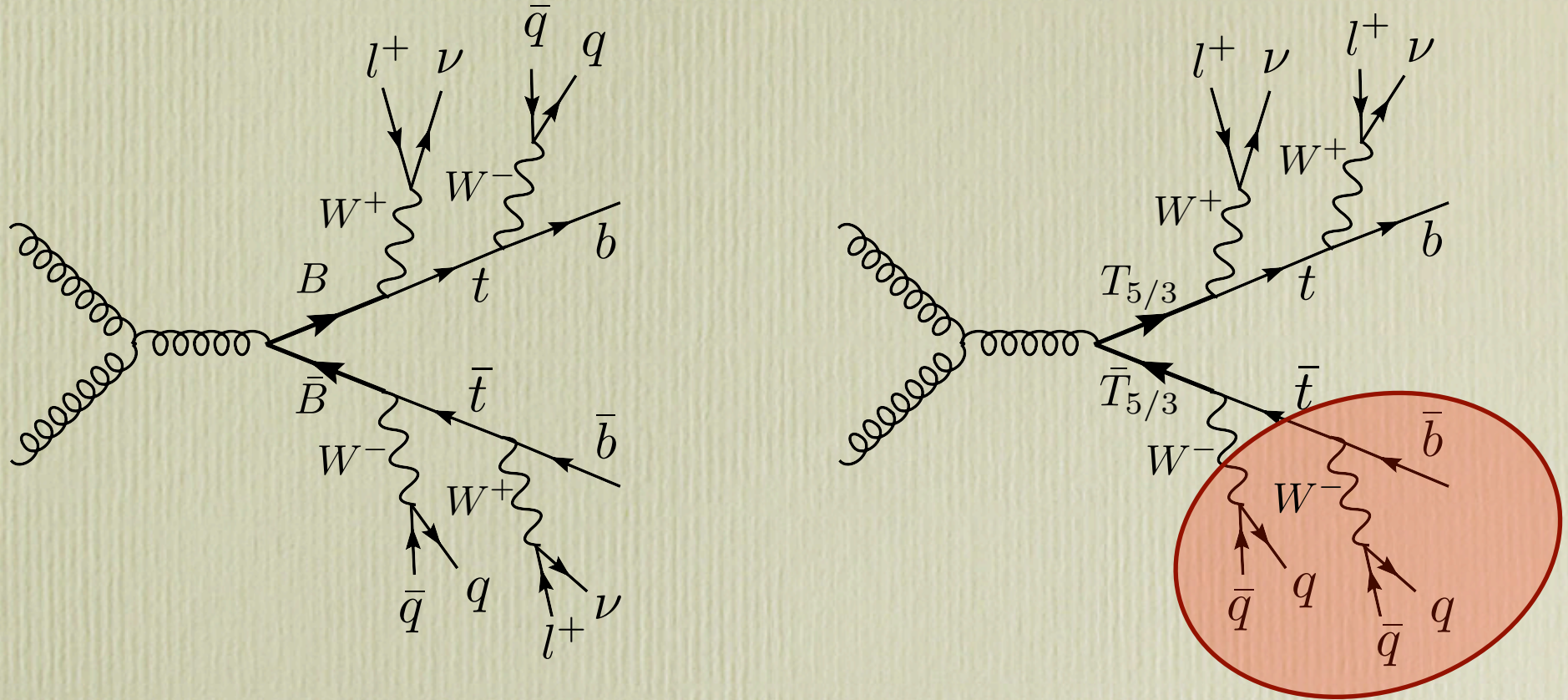
⊙ works only for heavy masses  $M_B \gtrsim 1 \text{ TeV}$

⊙ results depend on the jet energy algorithm used



👉 look for  $B\bar{B}$  and  $T_{5/3}\bar{T}_{5/3}$  in same-sign dilepton final states

[ R.C., G.Servant arXiv:0801.1679 ]



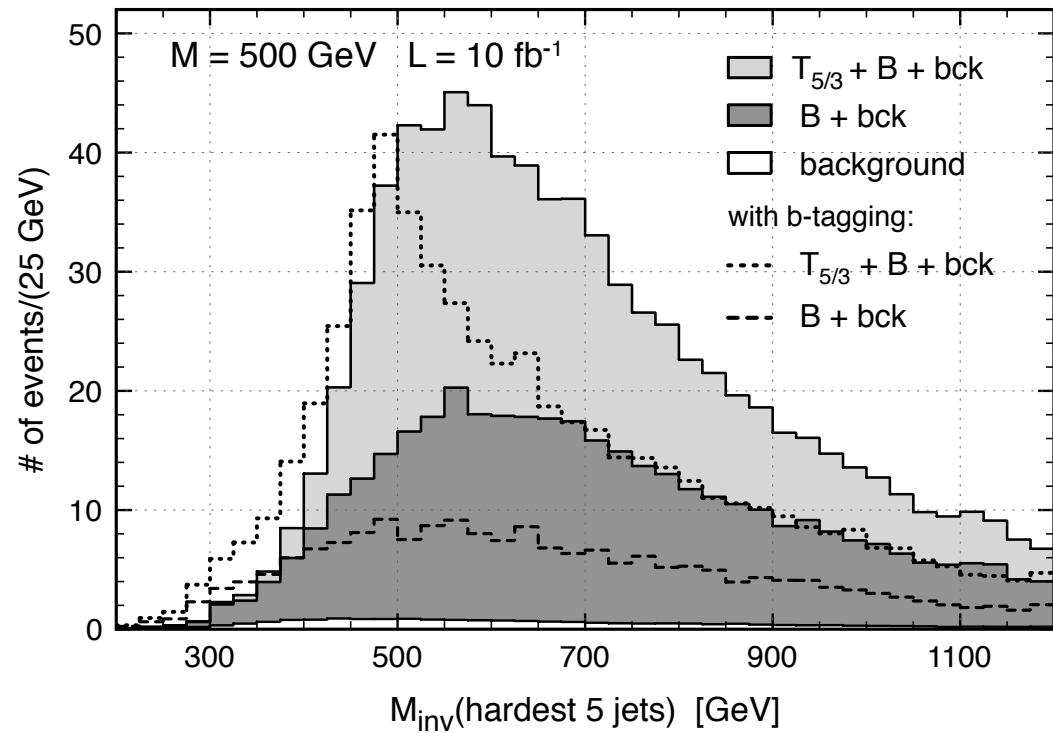
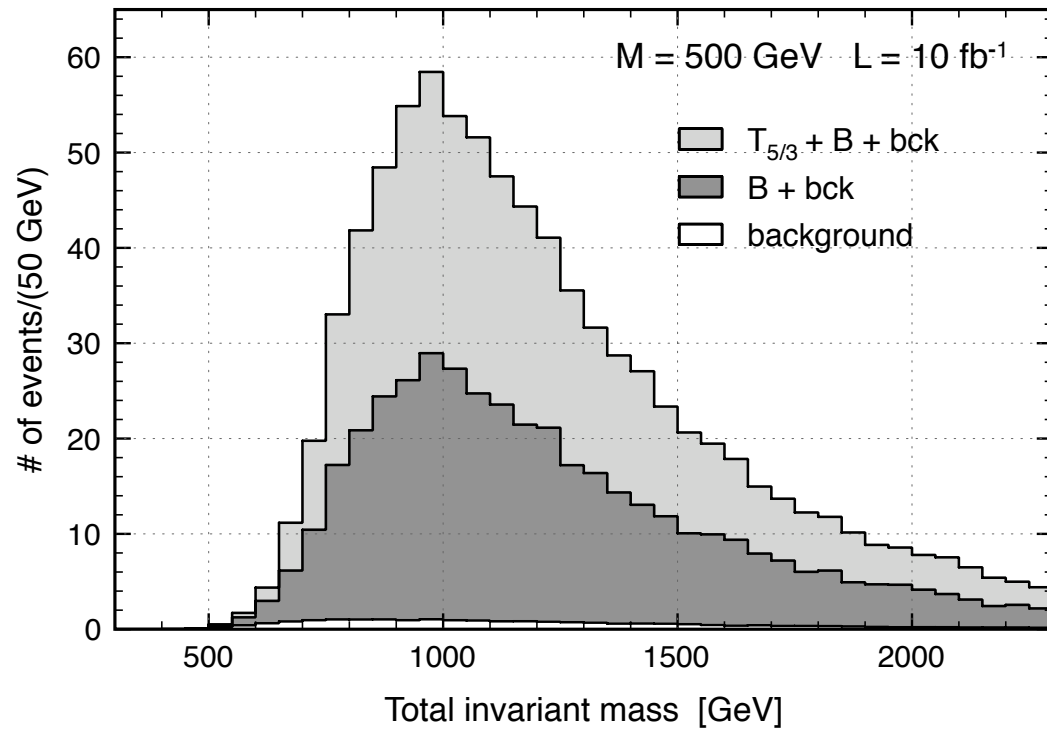
✓  $t\bar{t} + jets$  is not a background anymore [except for charge mis-ID]

✓ For the  $T_{5/3}$  case one can reconstruct the resonant ( $tW$ ) invariant mass

Cuts:

$$\underline{\text{jets}} : \begin{cases} p_T(1\text{st}) \geq 100 \text{ GeV} \\ p_T(2\text{nd}) \geq 80 \text{ GeV} \\ n_{jet} \geq 5, \quad |\eta_j| \leq 5 \end{cases}$$

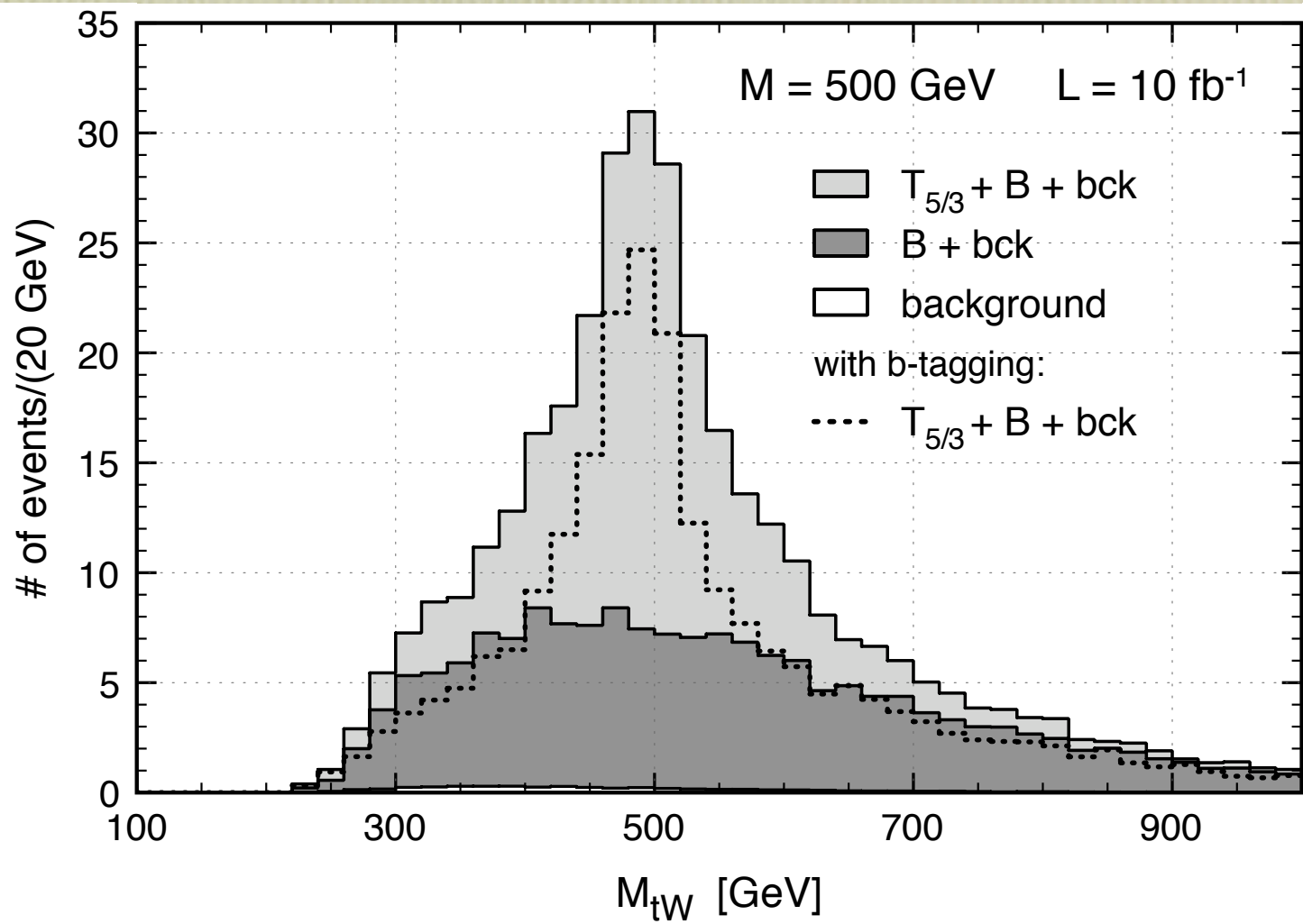
$$\underline{\text{leptons}} : \begin{cases} p_T(1\text{st}) \geq 50 \text{ GeV} \\ p_T(2\text{nd}) \geq 25 \text{ GeV} \\ |\eta_l| \leq 2.4, \quad \Delta R_{lj} \geq 0.4 \end{cases} \quad \cancel{E}_T \geq 20 \text{ GeV}$$



Discovery Potential:

		$I_{disc}$
$M = 500 \text{ GeV}$	$T_{5/3} + B$	56 $\text{pb}^{-1}$
	$B$ only	147 $\text{pb}^{-1}$

less than  
100  $\text{pb}^{-1}$



Backup slides

# Signal and Background Simulation

Signal and SM background have been simulated using:

- ❖ MadGraph/MadEvent [MatrixElement] + Pythia [Showering - no hadronization or und.event]
- ❖ Quark/Jet matching a la MLM
- ❖ Jets reconstructed with a cone algorithm (GetJet) with  $\Delta R = 0.4$  ,  $E_T^{min} = 30$  GeV
- ❖ Jet energy and momentum smeared by  $100\%/\sqrt{E}$  to simulate the detector resolution

	$\sigma$ [fb]	$\sigma \times BR(l^\pm l^\pm)$ [fb]
$T_{5/3}\bar{T}_{5/3}/B\bar{B} + jets$ ( $M = 500$ GeV)	$2.5 \times 10^3$	104
$T_{5/3}\bar{T}_{5/3}/B\bar{B} + jets$ ( $M = 1$ TeV)	37	1.6
$t\bar{t}W^+W^- + jets$ ( $\supset t\bar{t}h + jets$ )	121	5.1
$t\bar{t}W^\pm + jets$	595	18.4
$W^+W^-W^\pm + jets$ ( $\supset hW^\pm + jets$ )	603	18.7
$W^\pm W^\pm + jets$	340	15.5

SM bckg  
[ $m_h = 180$  GeV]

## other backgrounds:

- ★ Events where one lepton comes from a b-decay

these leptons are soft: completely removed by our cut  $p_T(l) \geq 25 \text{ GeV}$

- ★  $t\bar{t} + jets$  events where the charge of one lepton is mis-identified

charge mis-ID probability  $\epsilon_{mis}$  strongly depends on the lepton's  $p_T$  and  $\eta$

for  $t\bar{t} + jets$  the hardest lepton has  $p_T(l) \sim 100 \text{ GeV}$

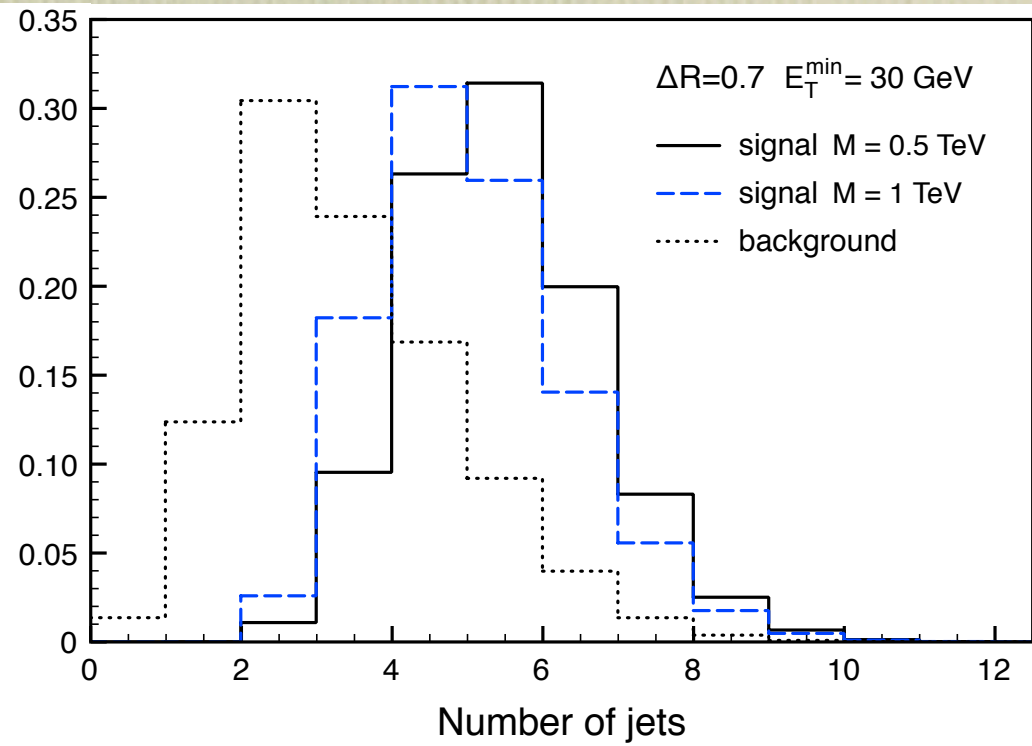
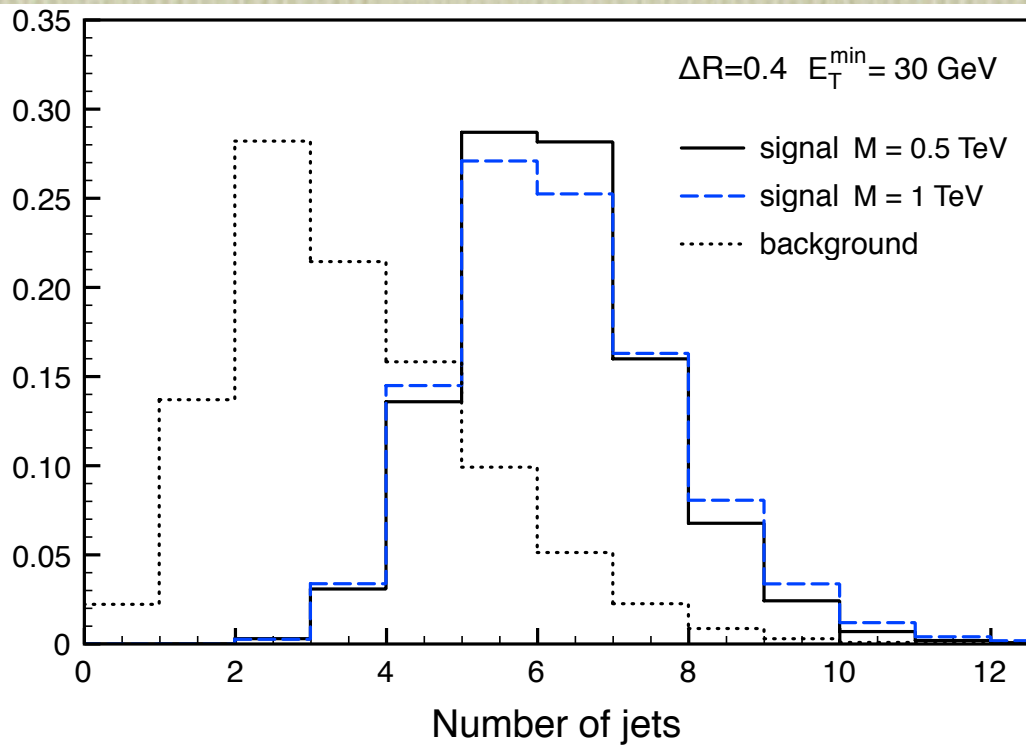
→  $\epsilon_{mis} \sim 10^{-4}$  seems possible →  $t\bar{t} + jets$  negligible

- ★  $Wl^+l^- + jets$  events where one lepton is lost

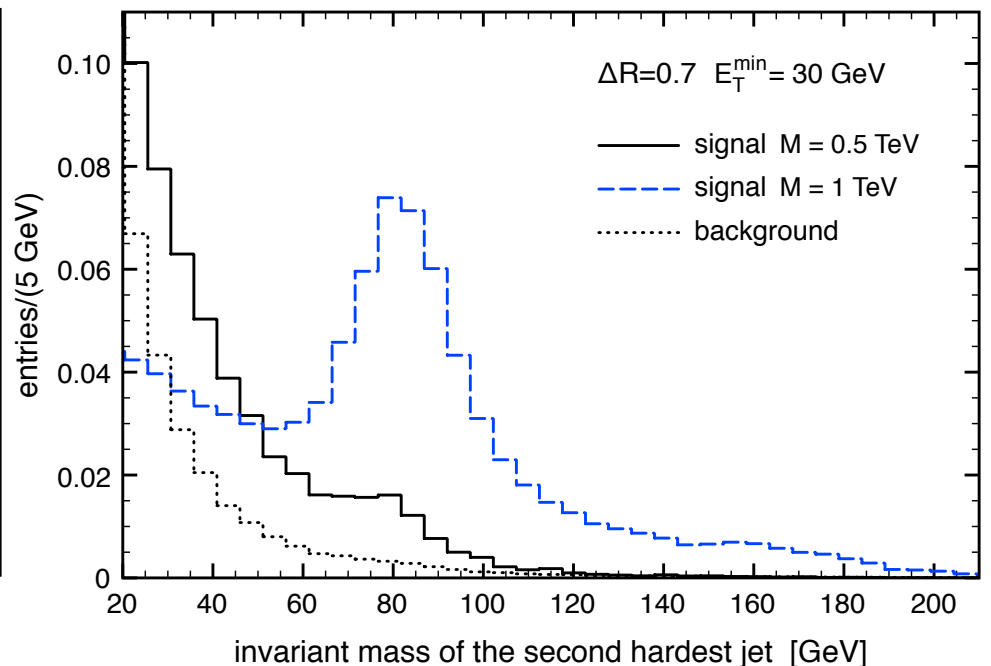
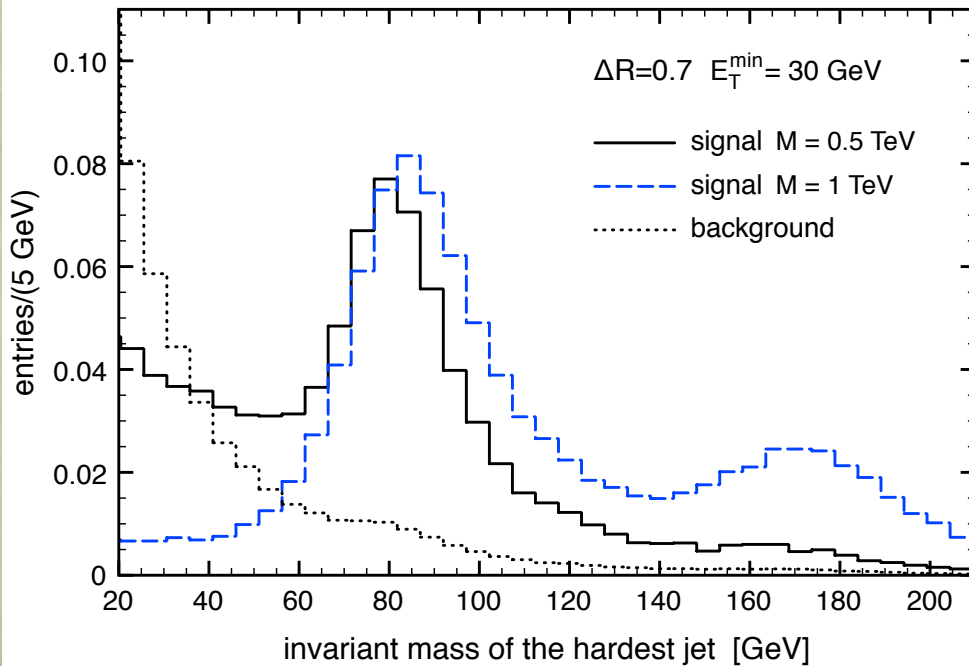
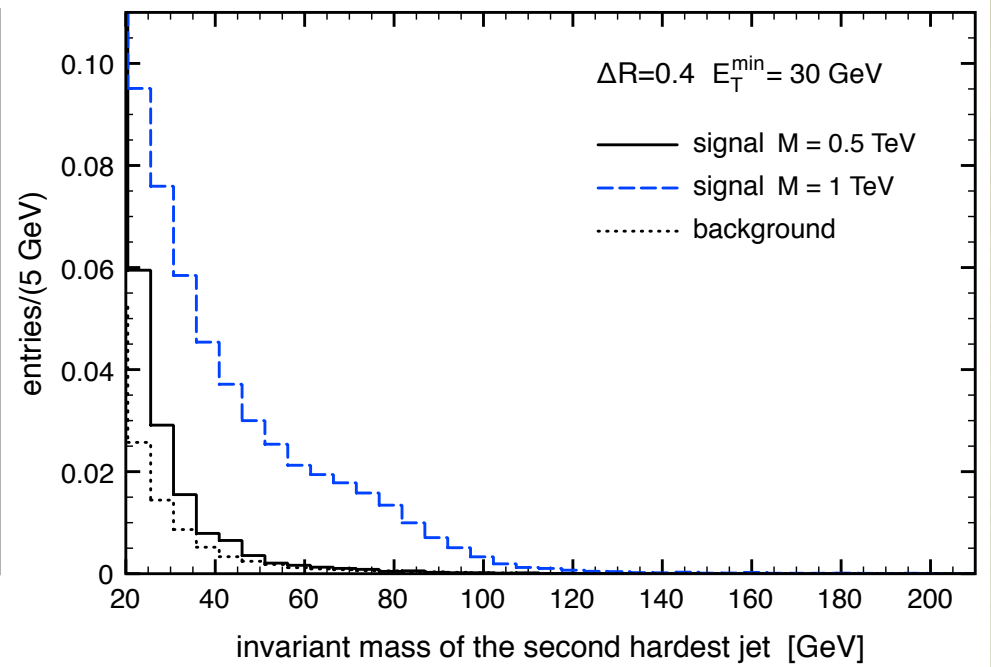
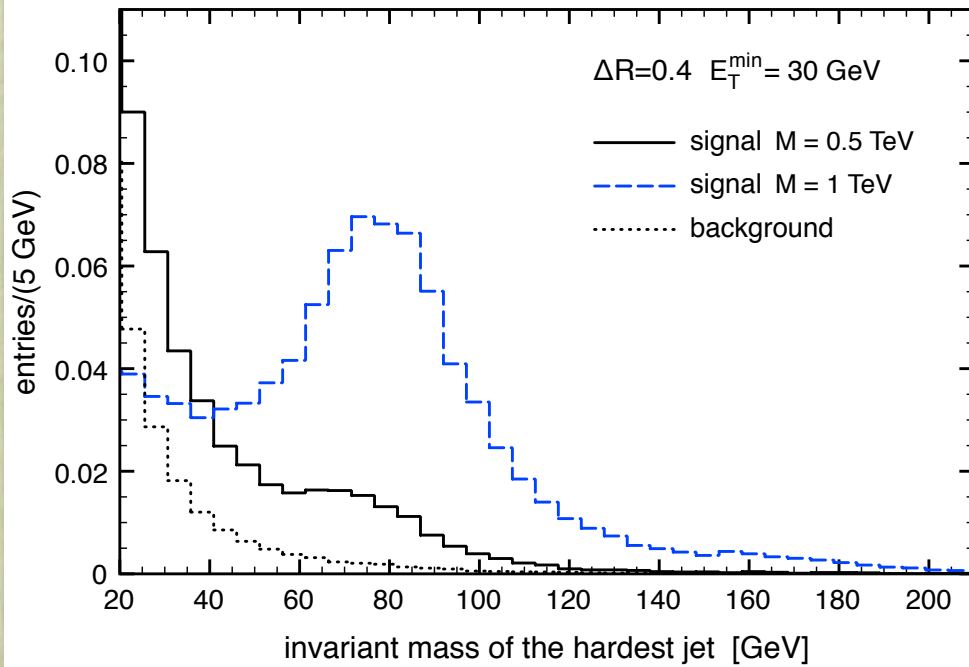
technically difficult to simulate with all the needed jets

→ we estimate it to be  $\lesssim 30\%$  of the sum of the included backgrounds

# # jets - with two different cone sizes



# jet invariant mass with two different cone sizes





# Strategy and main cuts

- ★ For  $\Delta R = 0.4$  only the  $M=1$  TeV signal has one “double” jet from boosted  $W$ 's
- ★ We demand at least 5 hard jets ( $p_T \geq 30$  GeV):  $l^\pm l^\pm + n \text{ jets} + \cancel{E}_T$  ( $n \geq 5$ )
- ★ Reference luminosities:  $10 \text{ fb}^{-1}$  for  $M = 500$  GeV  
 $100 \text{ fb}^{-1}$  for  $M = 1$  TeV

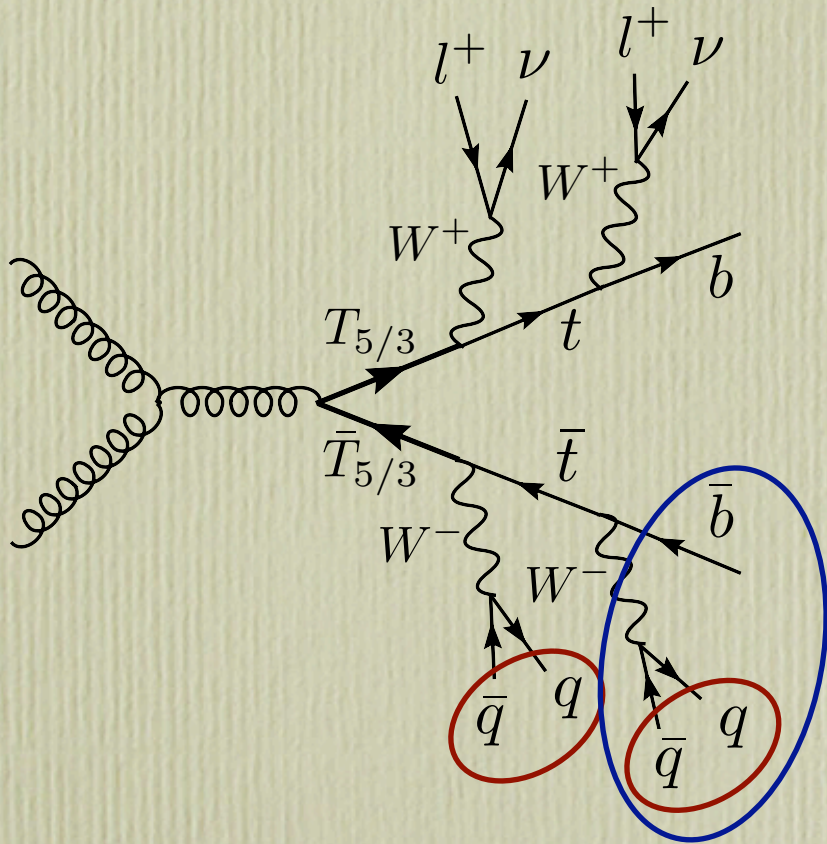
## Main Cuts:

$$\begin{array}{l}
 \underline{\text{jets}} : \begin{cases} p_T(1\text{st}) \geq 100 \text{ GeV} \\ p_T(2\text{nd}) \geq 80 \text{ GeV} \\ n_{jet} \geq 5, \quad |\eta_j| \leq 5 \end{cases} \\
 \underline{\text{leptons}} : \begin{cases} p_T(1\text{st}) \geq 50 \text{ GeV} \\ p_T(2\text{nd}) \geq 25 \text{ GeV} \\ |\eta_l| \leq 2.4, \quad \Delta R_{lj} \geq 0.4 \end{cases} \quad \cancel{E}_T \geq 20 \text{ GeV}
 \end{array}$$

	signal ( $M = 500$ GeV)	signal ( $M = 1$ TeV)	$t\bar{t}W$	$t\bar{t}WW$	$WWW$	$W^\pm W^\pm$
Efficiencies ( $\epsilon_{main}$ )	0.42	0.43	0.074	0.12	0.008	0.01
$\sigma$ [fb] $\times BR \times \epsilon_{main}$	44.2	0.67	1.4	0.62	0.15	0.16

# Mass Reconstruction

$M=500 \text{ GeV}$



## 1. Reconstruct 2 W's

$$|M(jj) - m_W| \leq 20 \text{ GeV}$$

$$\Delta R_{jj}(\text{1st pair}) \leq 1.5$$

$$|\vec{p}_T(\text{1st pair})| \geq 100 \text{ GeV}$$

$$\Delta R_{jj}(\text{2nd pair}) \leq 2.0$$

$$|\vec{p}_T(\text{2nd pair})| \geq 30 \text{ GeV}$$

## 2. Reconstruct 1 top ( $t=Wj$ )

$$|M(Wj) - m_t| \leq 25 \text{ GeV}$$

	signal ( $M = 500 \text{ GeV}$ )	$t\bar{t}W$	$t\bar{t}WW$	$WWW$	$WW$
$\epsilon_{2W}$	0.62	0.36	0.49	0.29	0.15
$\epsilon_{top}$	0.65	0.56	0.64	0.35	0.35